FIELD-INDUCED PAIR DENSITY WAVE

MAGNETIC FIELD CONTROL OF CUPRATE DENSITY WAVE

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T. Wu et al, Nature 477, 191 (2011)

J. Chang et al., Nat. Phys. 8, 871 (2012)

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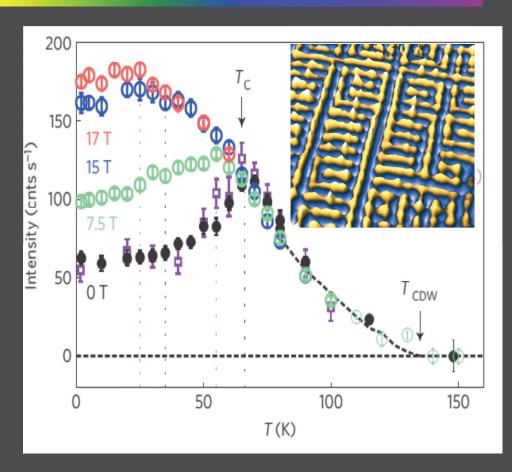
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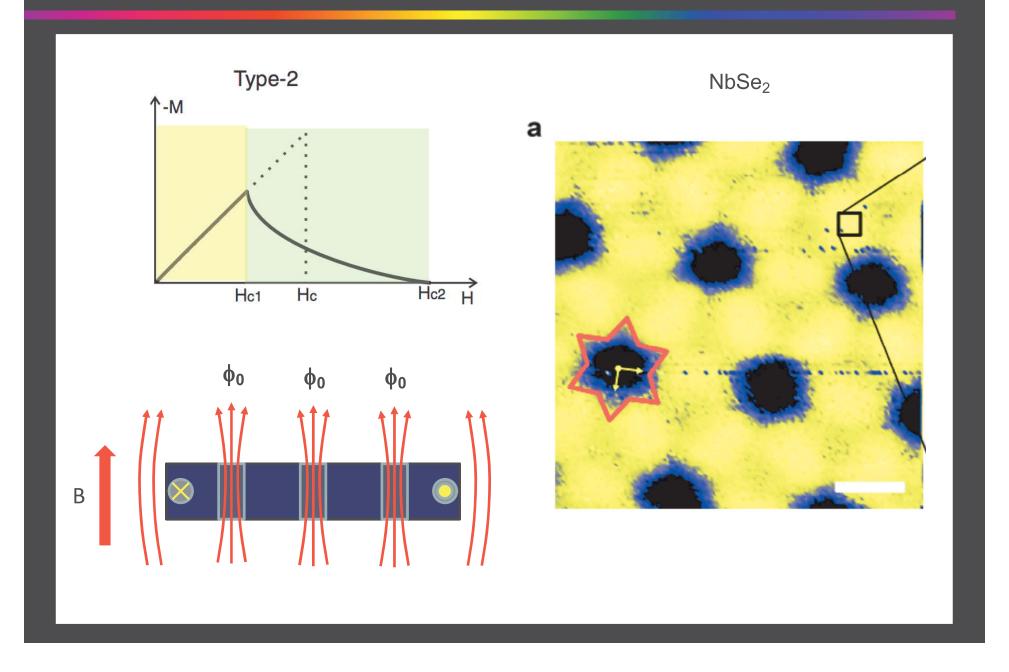
H. Jang et al. PNAS 113 14645–14650 (2016)



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CDW
$$\langle c_{k\uparrow}^{\dagger}, c_{k+Q_C}^{\dagger} \rangle$$
 or PDW $\langle c_{k\uparrow}^{\dagger}, c_{-k+Q_P}^{\dagger} \rangle$

SUPERCONDUCTOR+MAGNETIC FIELD => VORTEX LATTICE



PAIR DENSITY WAVE INDUCED AT VORTEX

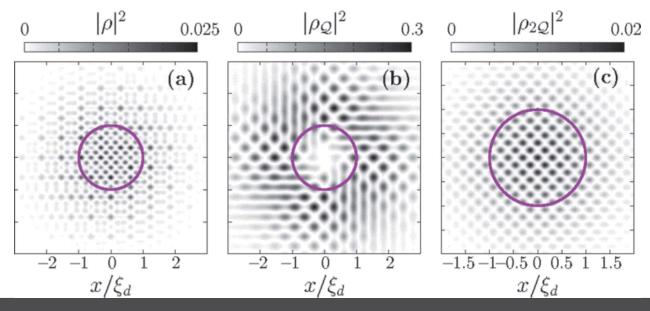
PHYSICAL REVIEW B 91, 104512 (2015)

Checkerboard order in vortex cores from pair-density-wave superconductivity

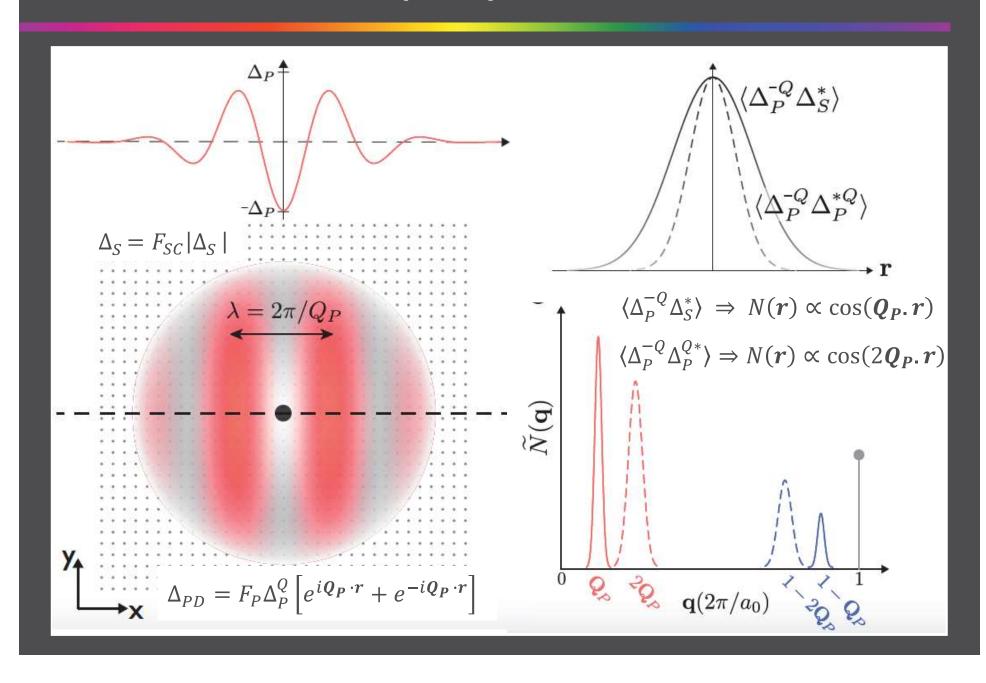
Daniel F. Agterberg¹ and Julien Garaud^{2,*}

¹Department of Physics, University of Wisconsin-Milwaukee, Milwaukee, Wisconsin 53211, USA ²Department of Theoretical Physics, KTH-Royal Institute of Technology, Stockholm, SE-10691 Sweden (Received 16 December 2014; revised manuscript received 26 February 2015; published 16 March 2015)

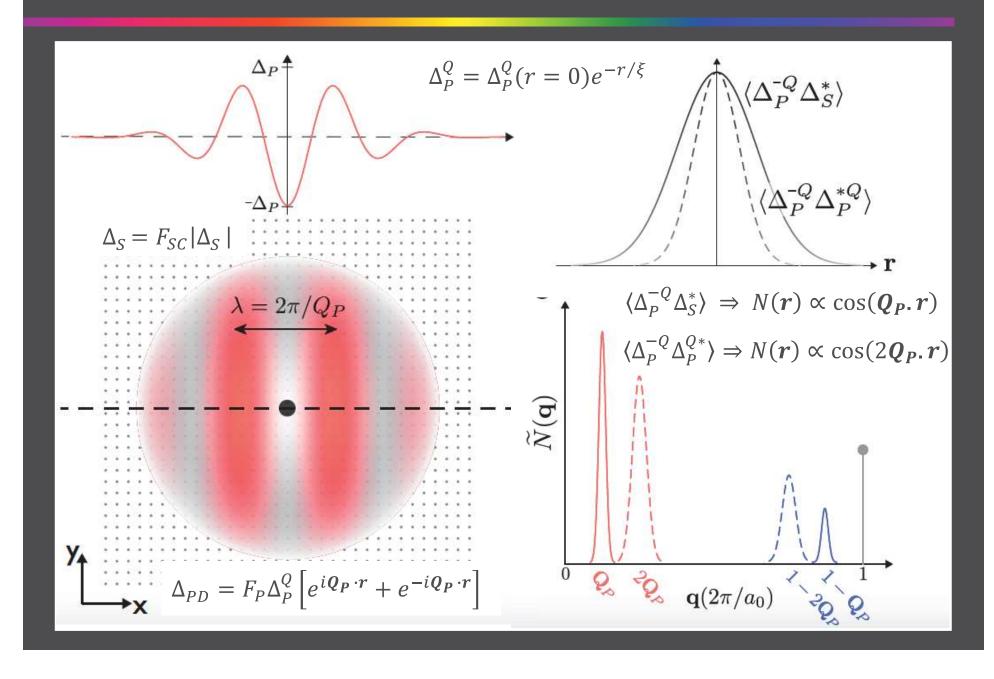
We consider competing pair-density-wave (PDW) and d-wave superconducting states in a magnetic field. We show that PDW order appears in the cores of d-wave vortices, driving checkerboard charge-density-wave (CDW) order in the vortex cores, which is consistent with experimental observations. Furthermore, we find an additional CDW order that appears on a ring outside the vortex cores. This CDW order varies with a period that is twice that of the checkerboard CDW and it only appears where both PDW and d-wave order coexist. The observation of this additional CDW order would provide strong evidence for PDW order in the pseudogap phase of the cuprates. We further argue that the CDW seen by nuclear magnetic resonance at high fields is due to a PDW state that emerges when a magnetic field is applied.



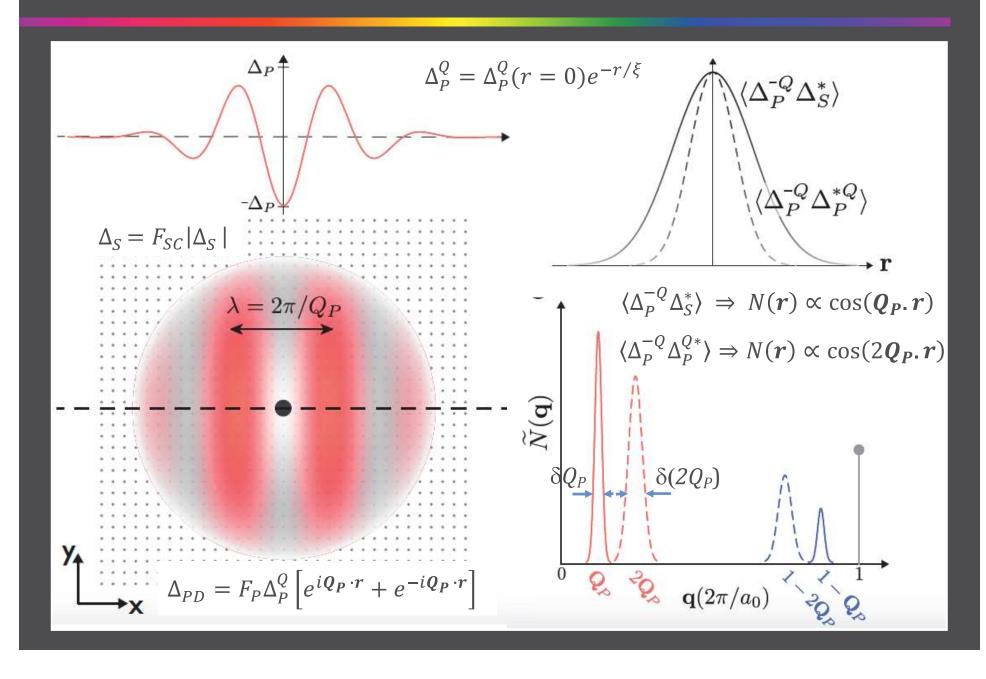
PDW IN VORTEX HALO $\Rightarrow Q_P \& 2Q_P$ CHARGE DENSITY MODULATIONS



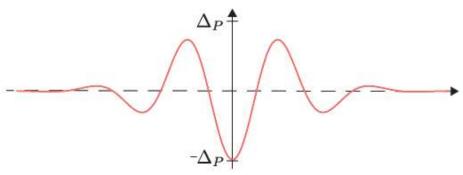
PDW IN VORTEX HALO $\Rightarrow Q_P \& 2Q_P$ MODULATION DECAY LENGTHS



PDW IN VORTEX HALO \Rightarrow LINEWIDTHS $\delta(2Q_P) = 2(\delta Q_P)$



PDW IN VORTEX HALO ⇒ EXPECTED PHENOMENOLOGY



$$\Delta_S = F_{SC} |\Delta_S|$$

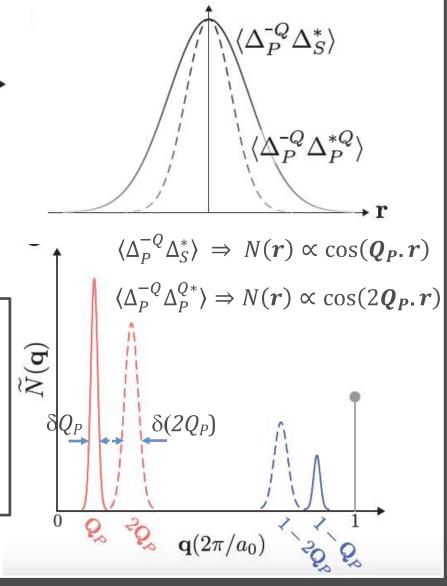
$$\Delta_P^Q = F_P |\Delta_P| \left[e^{iQ_P \cdot r} + e^{-iQ_P \cdot r} \right]$$

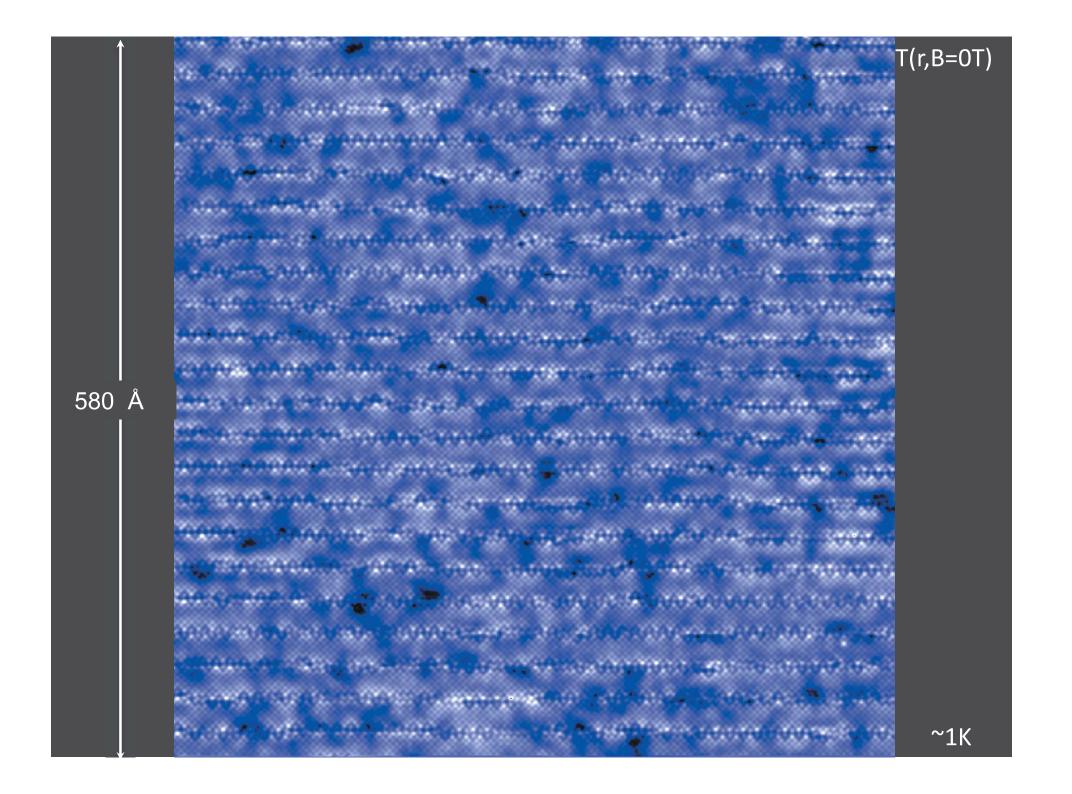
PDW Q_P WITHIN VORTEX HALO

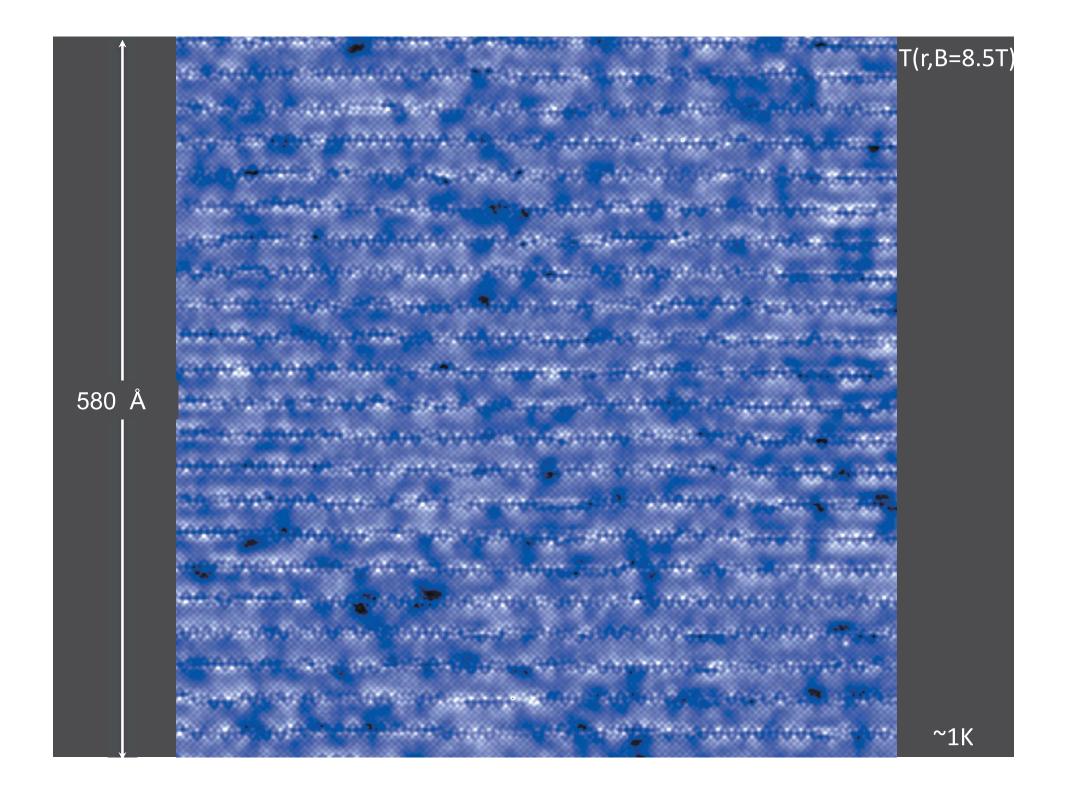
 $Q_P \& 2Q_P$ CHARGE DENSITY MODULATIONS

d-SYMMETRY PDW \Rightarrow s-SYMMETRY MODS

MODULATION LINEWIDTHS: $\delta(2Q_P) = 2(\delta Q_P)$

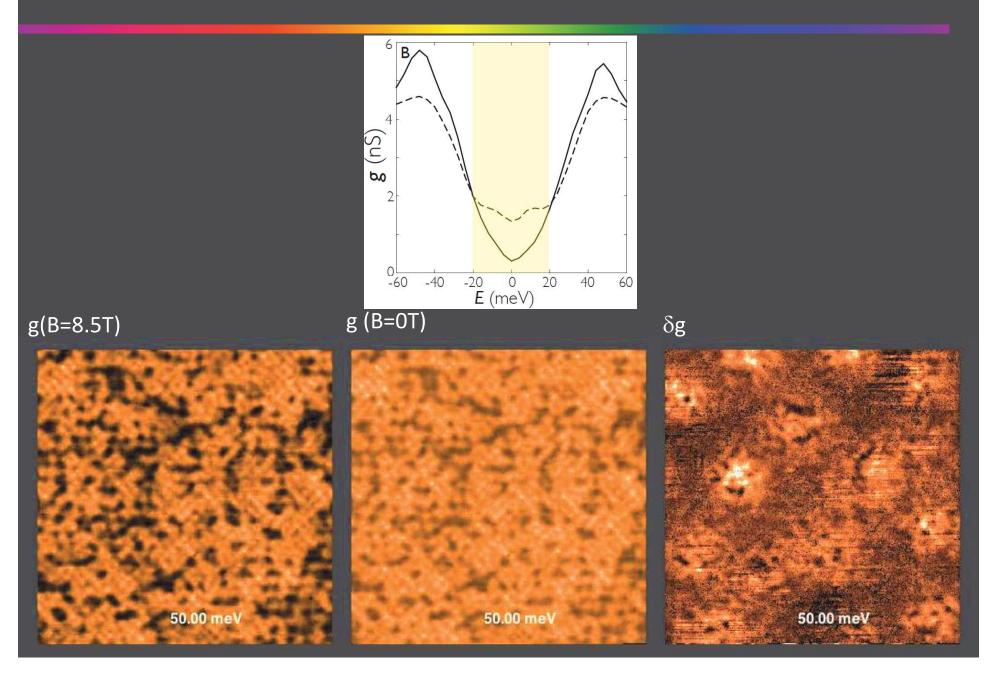




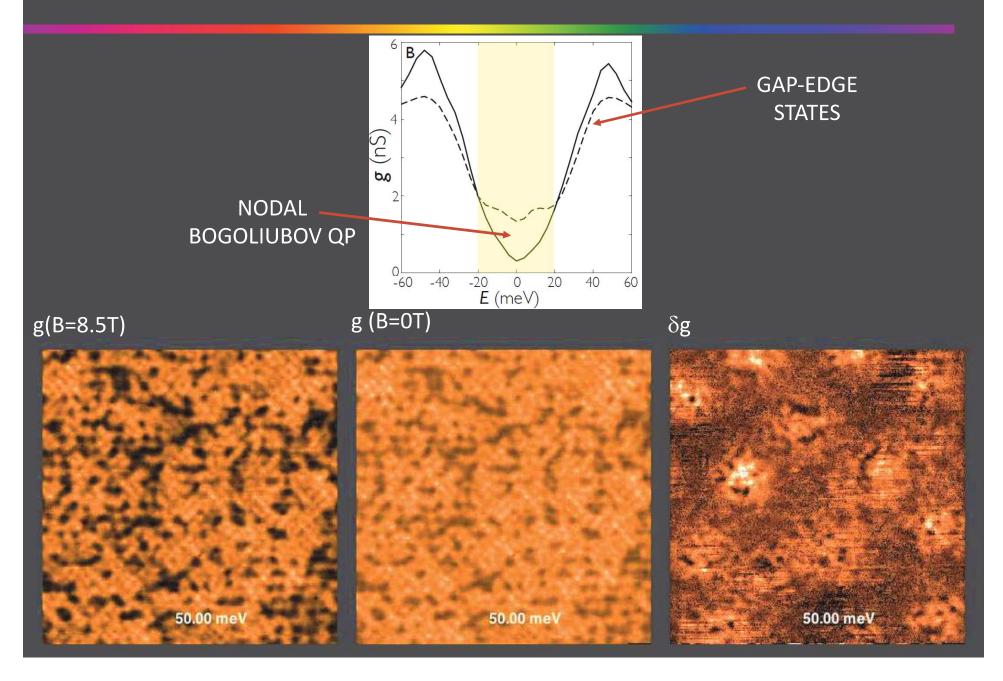




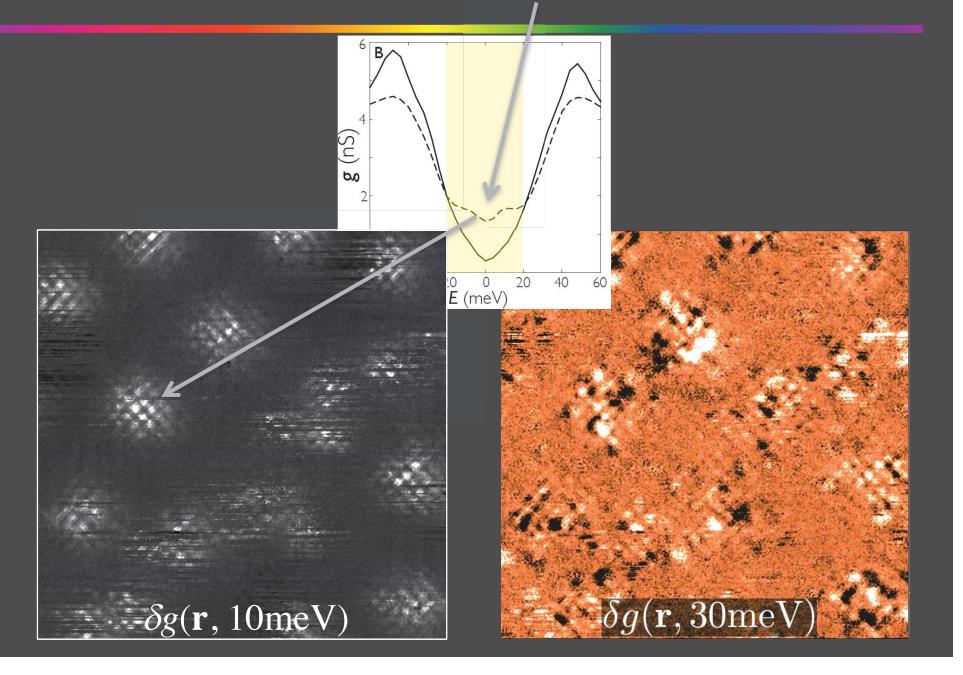
FIELD-INDUCED CHANGES TO ELECTRONIC STRUCTURE @ HALO



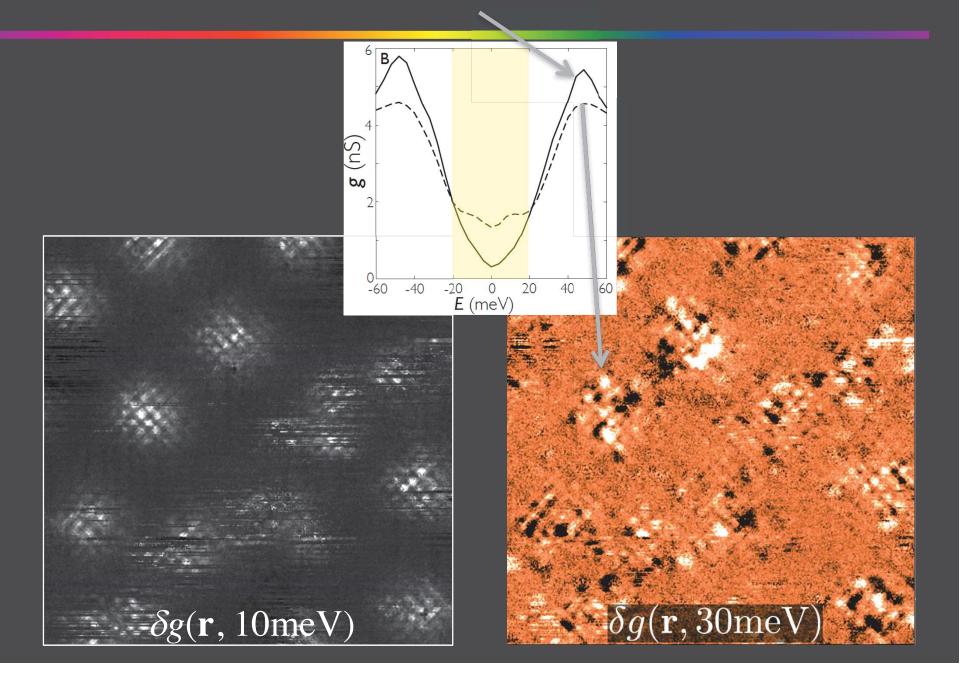
FIELD-INDUCED CHANGES TO ELECTRONIC STRUCTURE @ HALO



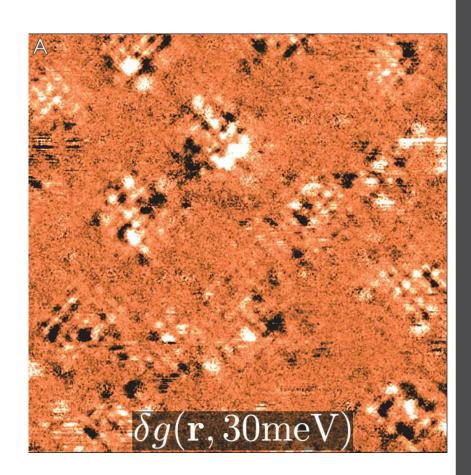
NODAL BOGOLIUBOV QUASIPARTICLES



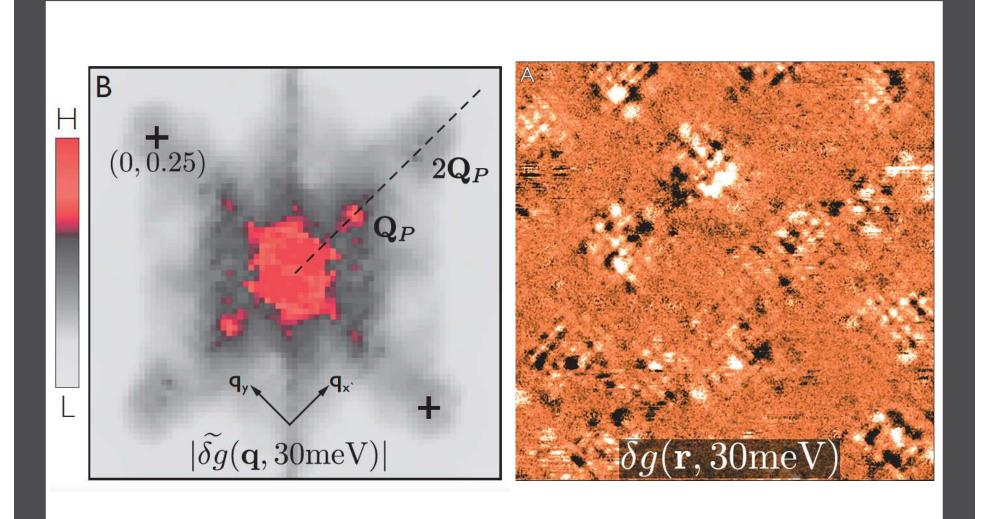
GAP EDGE STATES



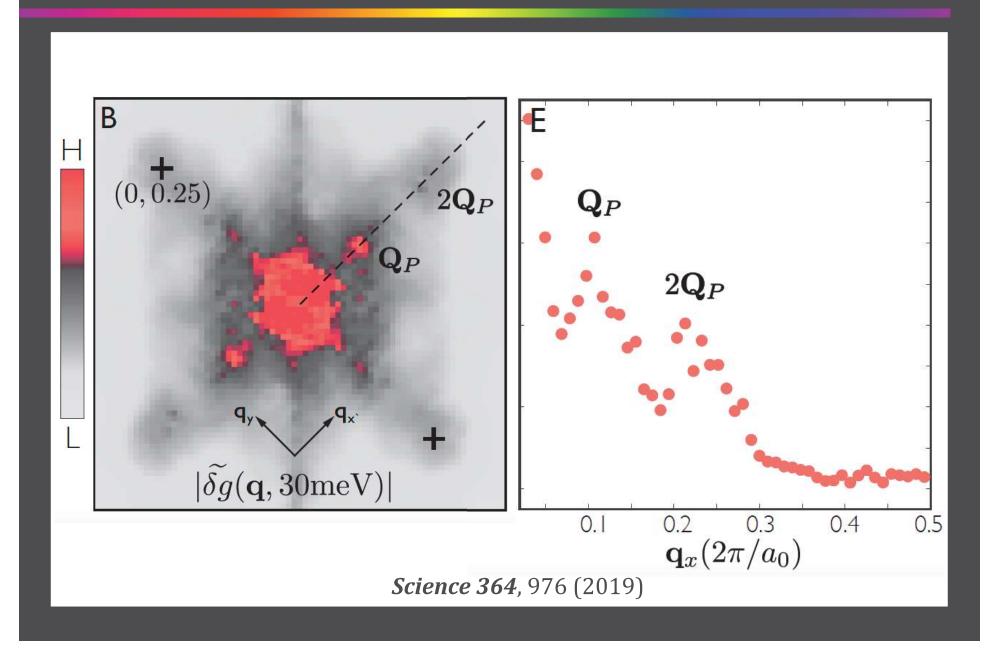
FIELD-INDUCED N(r) MODULATIONS



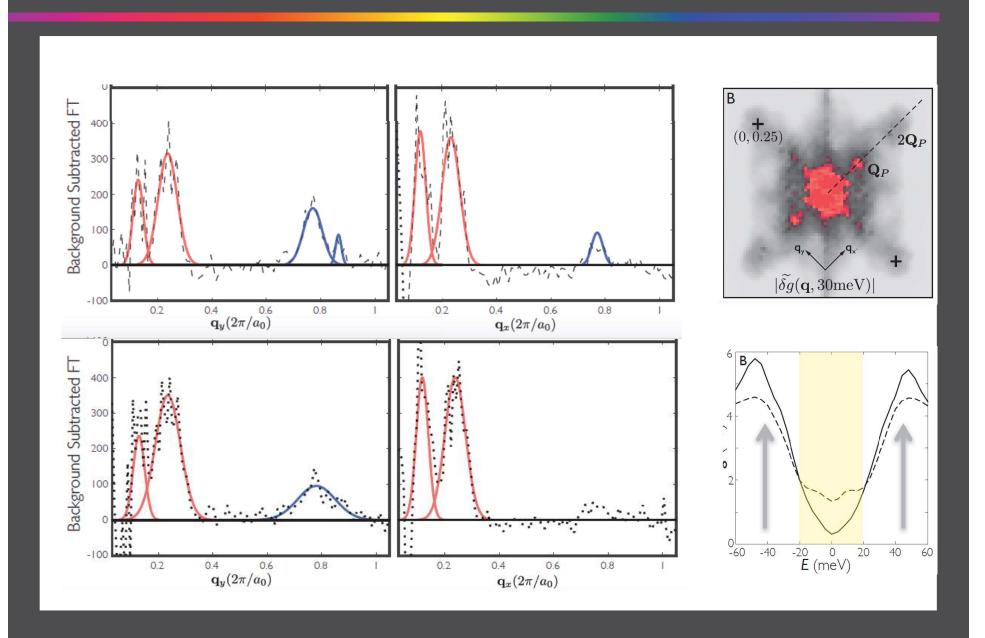
FIELD-INDUCED N(r) MODULATIONS



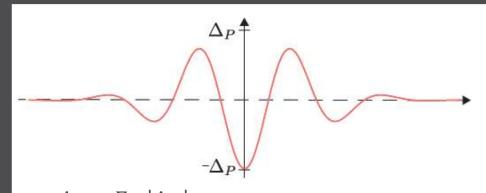
FIELD INDUCED N(r) MODULATIONS : PEAKS at Q_P and $\overline{Q_P}$



FIELD-INDUCED N(r) MODS Q_P AND $2Q_P \rightleftarrows \delta(2Q_P) \approx 2\delta(Q_P)$



PDW IN VORTEX HALO ⇒ EXPECTED PHENOMENOLOGY



$$\Delta_S = F_{SC} |\Delta_S|$$

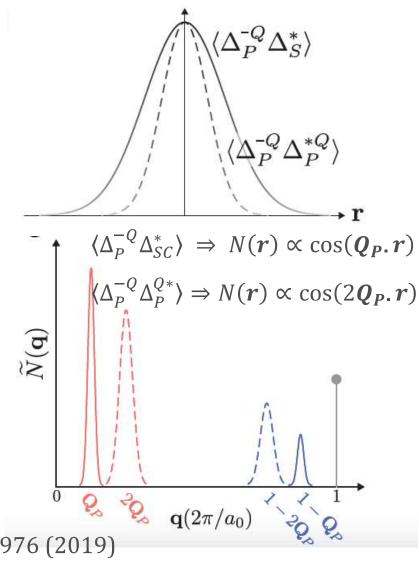
$$\Delta_{PD} = F_P \Delta_P^Q \left[e^{iQ_P \cdot r} + e^{-iQ_P \cdot r} \right]$$

PDW Q_P WITHIN VORTEX HALO

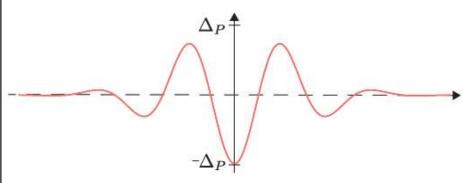
 $Q_P \& 2Q_P$ CHARGE DENSITY MODULATIONS

d-SYMMETRY PDW \Rightarrow s-SYMMETRY MODS

MODULATION LINEWIDTHS: $\delta(2Q_P) = 2(\delta Q_P)$



PDW IN VORTEX HALO ⇒ OBSERVED PHENOMENOLOGY



$$\Delta_S = F_{SC} |\Delta_S|$$

$$\Delta_{PD} = F_P \Delta_P^Q \left[e^{iQ_P \cdot r} + e^{-iQ_P \cdot r} \right]$$

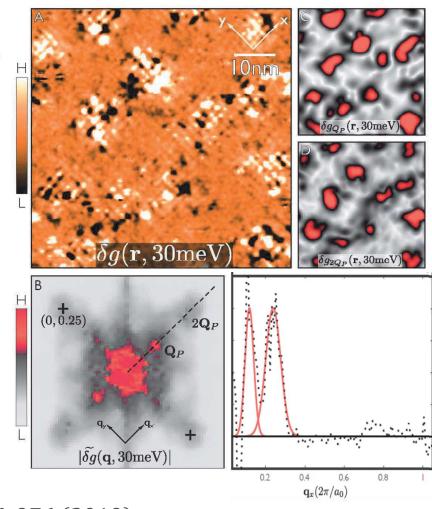
$\underline{PDW} Q_P \underline{WITHIN VORTEX HALO}$

 $Q_P \& 2Q_P$ CHARGE DENSITY MODULATIONS

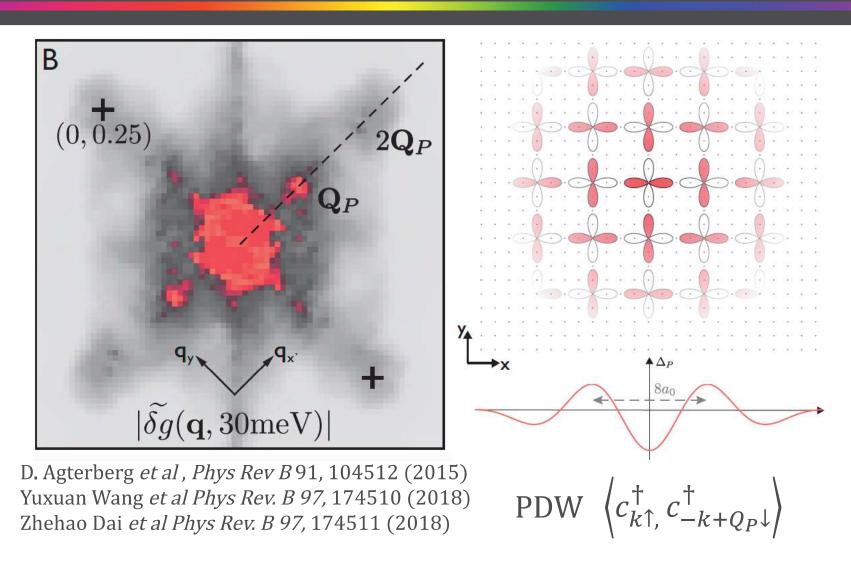
d-SYMMETRY PDW \Rightarrow s-SYMMETRY MODS

MODULATION LINEWIDTHS: $\delta(2Q_P) = 2(\delta Q_P)$

PARTICLE-HOLE SYMMETRY



BIAXIAL 8a₀ PDW INDUCED BY MAGNETIC FIELD



MAGNETIC FIELD CONTROL OF CUPRATE PDW

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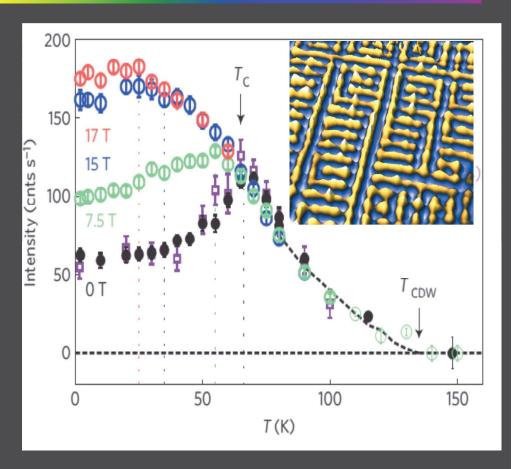
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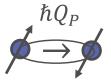


Chang *et al. Nat Phys* 8, 871 (2012)

PDW
$$\left\langle c_{k\uparrow}^{\dagger}, c_{-k+Q_P\downarrow}^{\dagger} \right\rangle$$

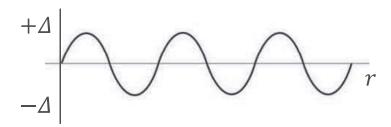
VISUALIZE PDW GAP MODULATION: $\Delta_0 cos(Q_P, r)$

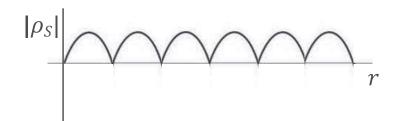
CUPRATE PDW GAP MODULATIONS



$$\left\langle c_{k\uparrow,}^{\dagger} c_{-k+Q_P\downarrow}^{\dagger} \right\rangle$$

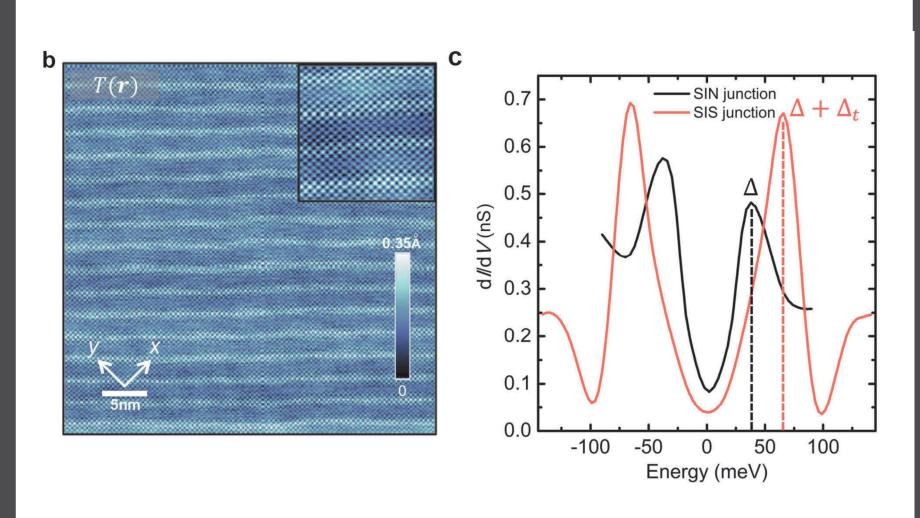
$$\Delta(r) = \Delta_P \left[e^{iQ_P \cdot r} + e^{-iQ_P \cdot r} \right]$$





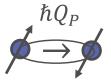


SIS SINGLE-PARTICLE TUNNELING



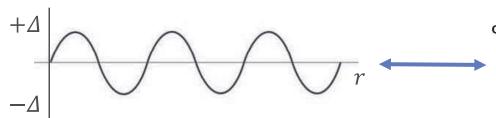
Kazuhiro Fujita et al (2019)

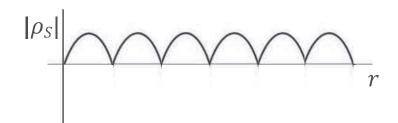
CUPRATE PDW GAP MODULATIONS



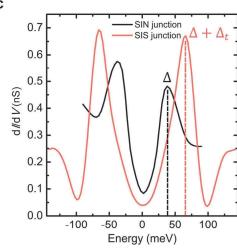
$$\left\langle c_{k\uparrow,}^{\dagger} c_{-k+Q_P\downarrow}^{\dagger} \right\rangle$$

$$\Delta(r) = \Delta_P \left[e^{iQ_P \cdot r} + e^{-iQ_P \cdot r} \right]$$



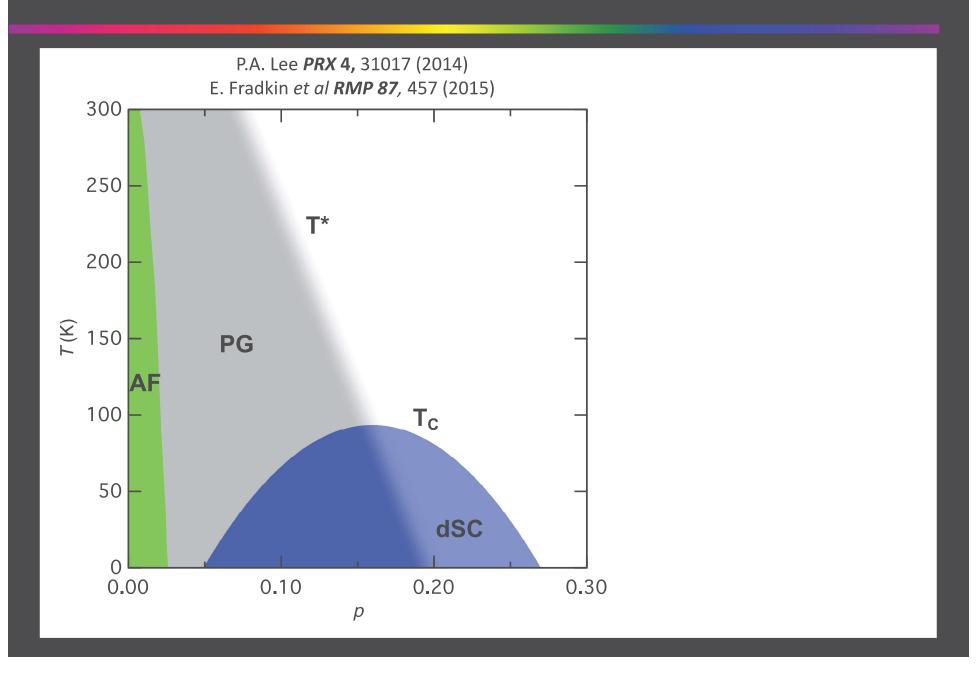




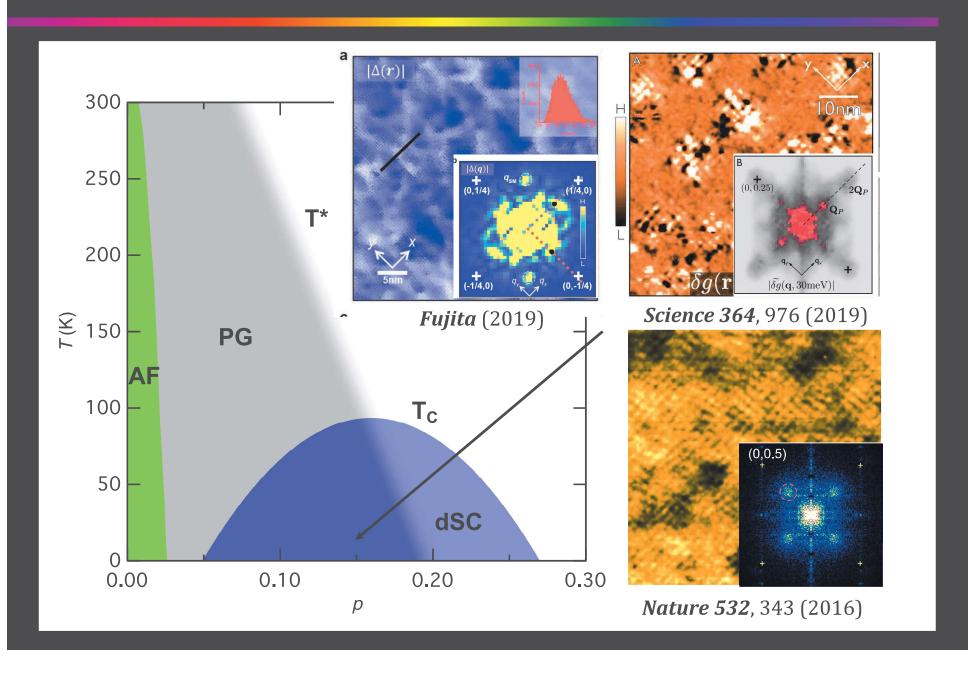


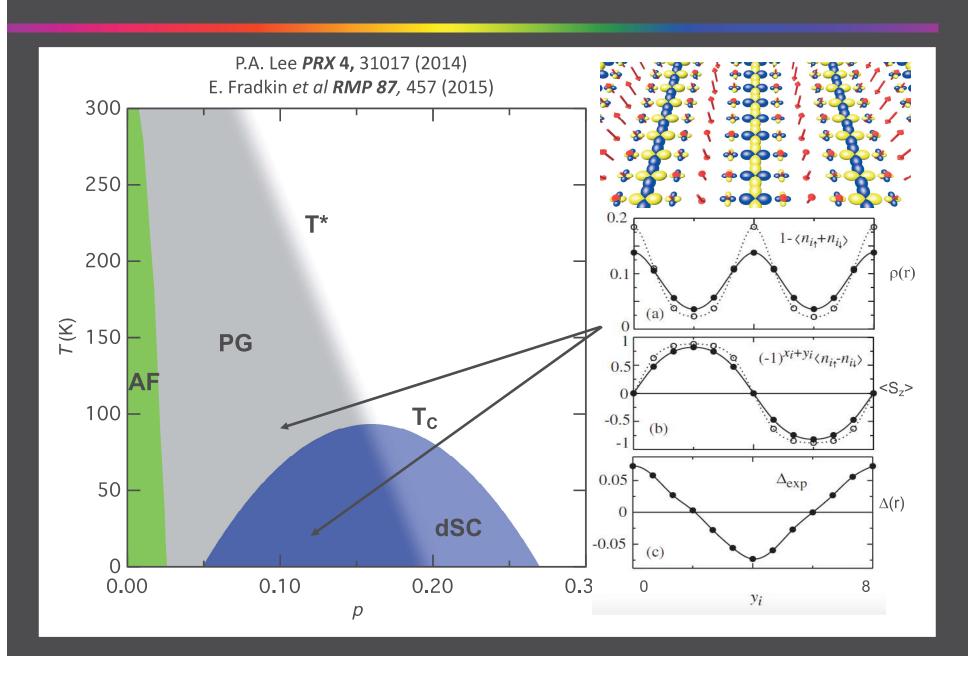
DISCUSSION

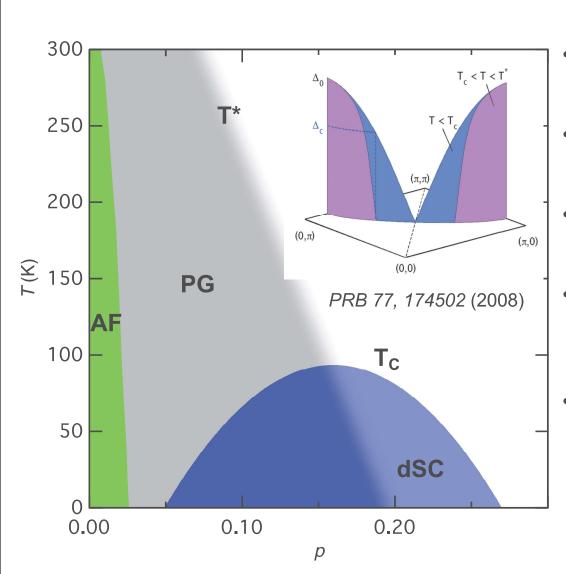
DOES STRONG-COUPLING PDW STATE EXIST IN CUPRATES?



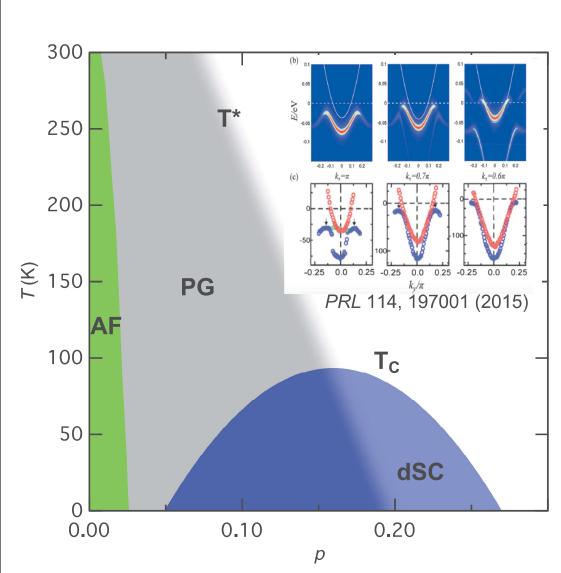
YES!



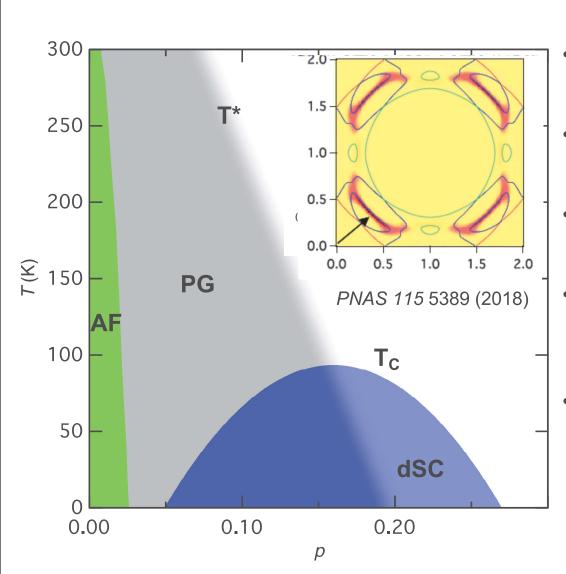




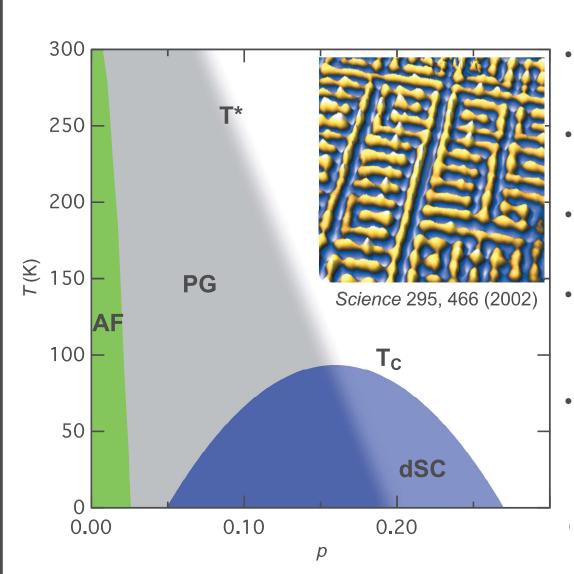
- PDW exhibits a particle-hole symmetric antinodal gap
- PDW gives the correct spectral functions for underdoped CuO₂
- PDW exhibits k-space 'Fermi Arc' of unbound electrons
- PDW yields small electron-like pocket with correct frequency of quantum oscillations
- PDW spin modulations at Q_P and charge modulations primarily at $2Q_P$.



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