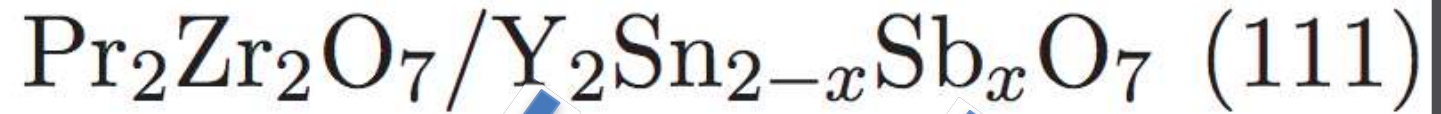


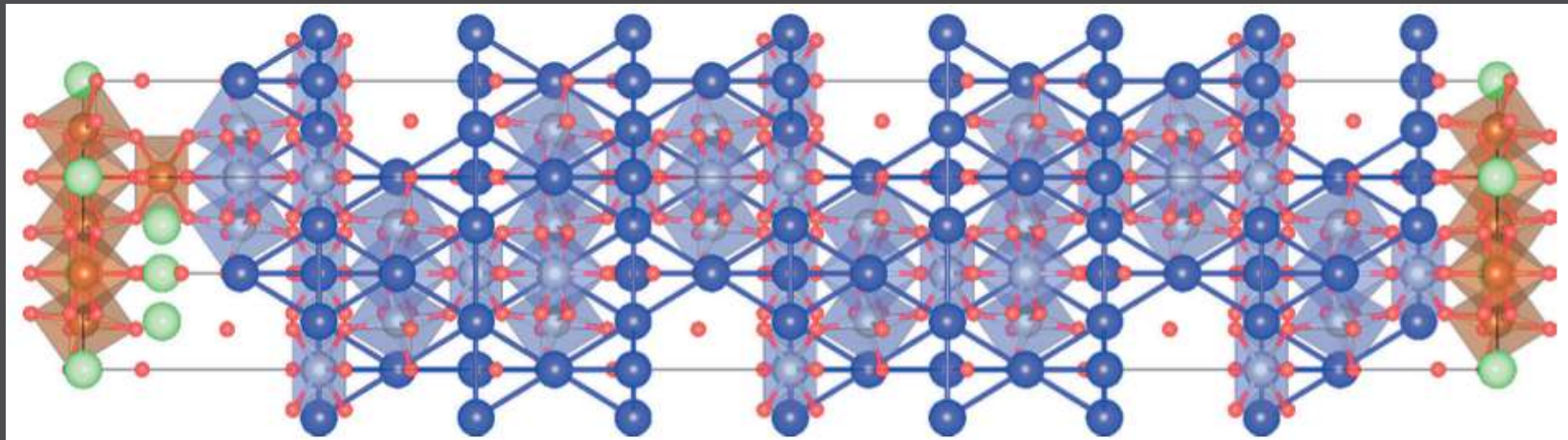
Interface Engineering?

# Epitaxial Heterostructure



Non-magnetic

s-electrons:  
large overlap,  
isotropic FS.

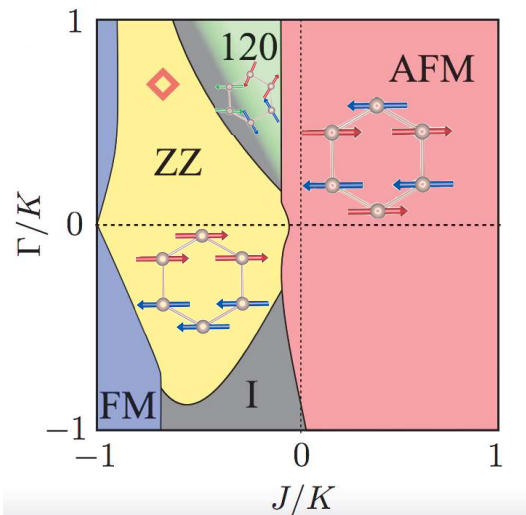


Other Quantum Paramagnets?

# $\alpha$ -RuCl<sub>3</sub>

- Layered spin-orbit assisted Mott insulator close to exotic quantum spin liquid ground state. Y.-J. Kim, K. S. Burch et al (2015)
- Candidate for honeycomb Kitaev model.

Alexei Kitaev (2006)



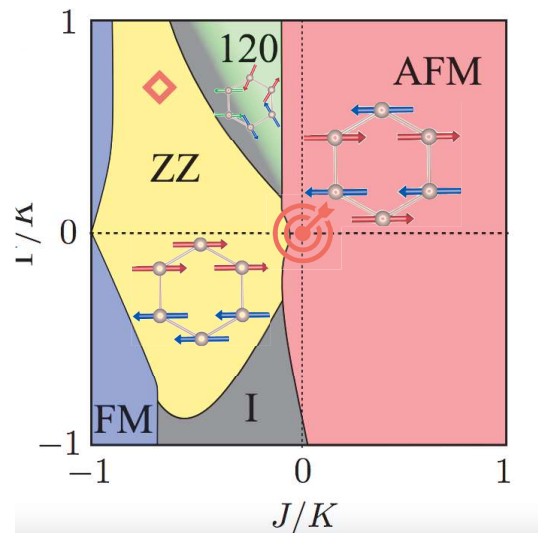
Kee et al (2015)

$$H = \sum_{\langle ij \rangle \in \alpha\beta(\gamma)} [K S_i^\gamma S_j^\gamma + J \mathbf{S}_i \cdot \mathbf{S}_j + \Gamma (S_i^\alpha S_j^\beta + S_i^\beta S_j^\alpha)]$$

# $\alpha$ -RuCl<sub>3</sub>

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Alexei Kitaev (2006)



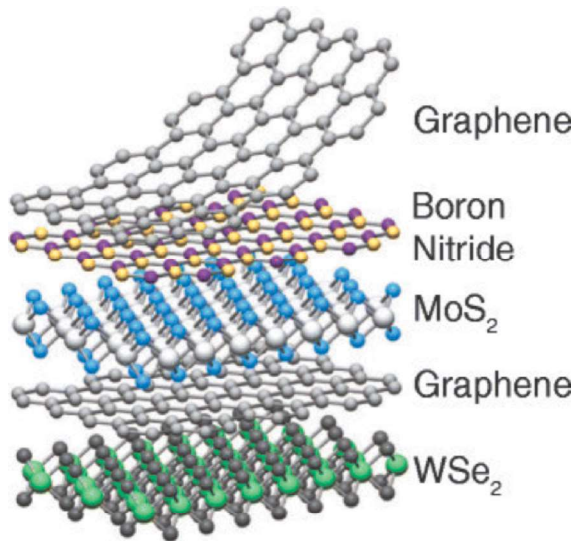
Kee et al (2015)

$$H = \sum_{\langle ij \rangle \in \alpha\beta(\gamma)} [K S_i^\gamma S_j^\gamma + J \mathbf{S}_i \cdot \mathbf{S}_j + \Gamma (S_i^\alpha S_j^\beta + S_i^\beta S_j^\alpha)]$$

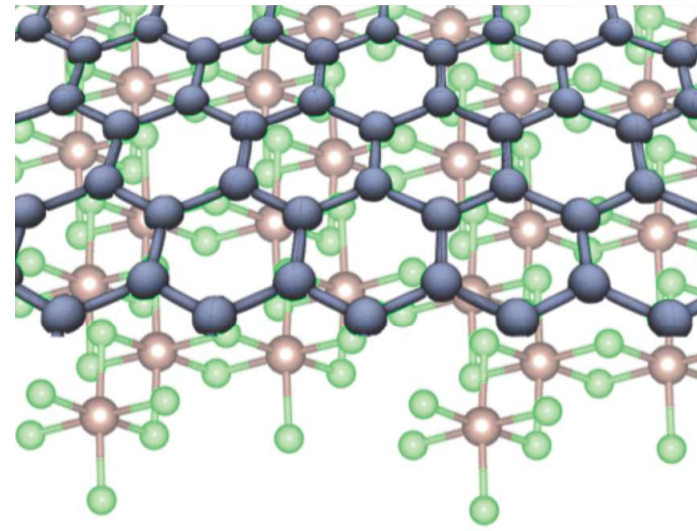
- Questions:
  - How to avoid ordering?
  - How to dope?

# Mismatched Hetero-interfaces

- Experimental/fabrication developments offer rich new phase space of lattice-mismatched hetero-vdW interfaces



Geim & Grigorieva (2013)



graphene on  $\alpha$ -RuCl<sub>3</sub>

$$\left. \begin{aligned} a_{\text{RuCl}_3} &= 5.96 \text{ \AA} \\ a_{\text{g}} &= 1.42 \text{ \AA} \end{aligned} \right\} \approx 123\% \text{ lattice mismatch.}$$

# Non-crystalline Interface?

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- Twisted Homo-interfaces
  - Twisted multi-layer graphene and TMD's.
  - Moire superlattice provide approximate periodicity.

—large supercell calculation with strain

: Mismatched Interface Theory (MINT), Gerber, Arias, EAK,  
arXiv: <https://arxiv.org/abs/1902.09550>

# Mismatched INterface Theory (MINT)

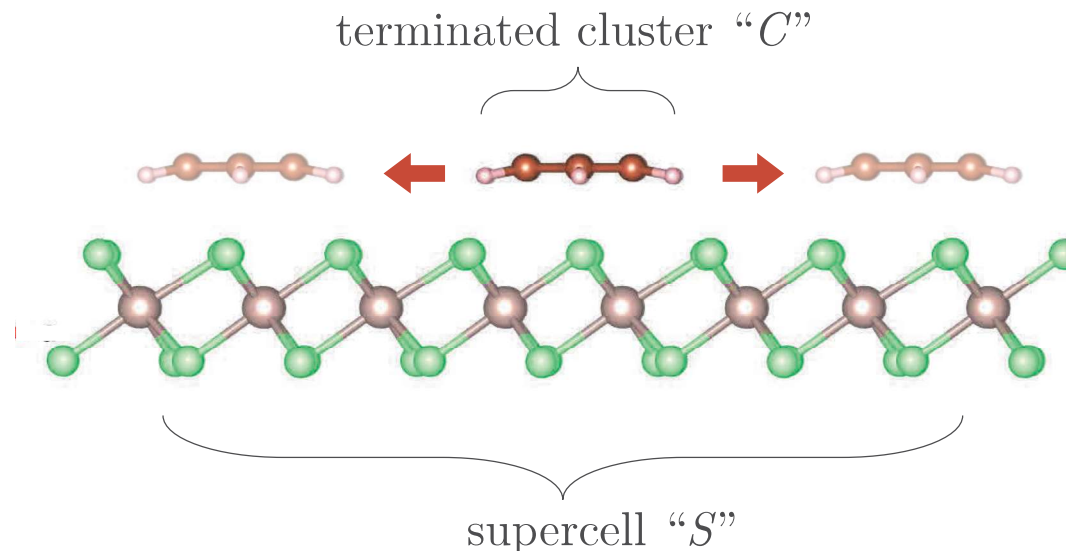
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**Step 1:** construct “MINT representation” of heterostructure using increasingly large clusters “ $C$ ” averaged over “ $S$ ”.

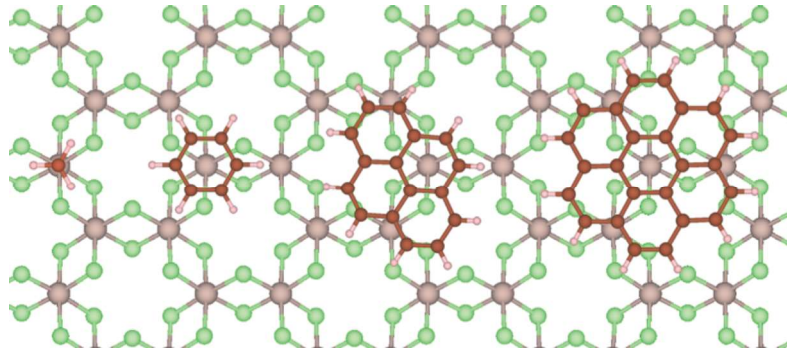
- Perform *ab initio* calculations for each reduced system.
- Scale to atomic density of ideal system, look for convergence.

**Step 2:** use this MINT representation, in which “ $C$ ” is replaced by its averaged impact on “ $S$ ”, to predict electronic properties of an infinite heterostructure.

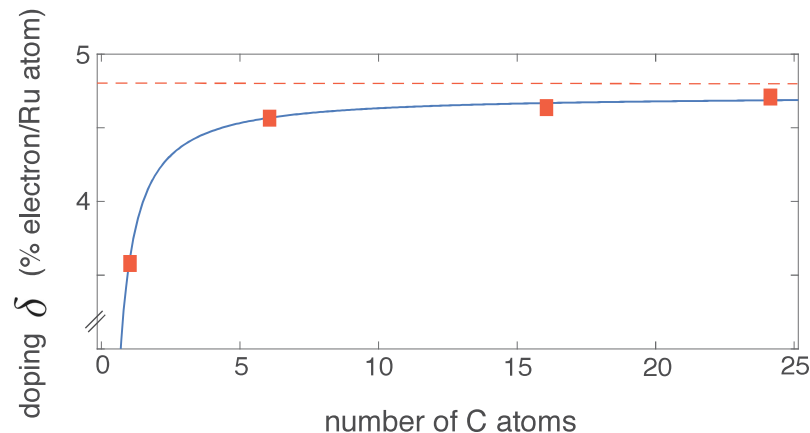




# MINT: graphene on $\alpha$ -RuCl<sub>3</sub> (doping)



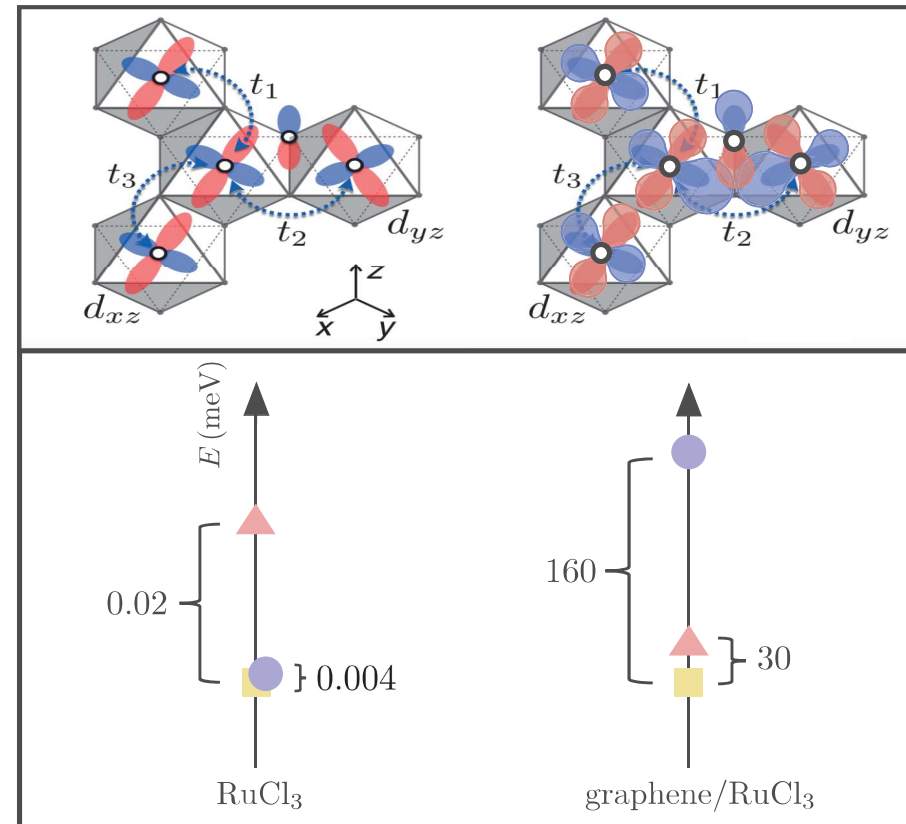
- Compute *ab initio* charge densities for each cluster averaged over RuCl<sub>3</sub> plane.



- Scale to atomic ratio of C/Ru=5.86, extrapolate doping for ideal heterostructure to construct MINT representation.

# MINT: graphene on $\alpha$ -RuCl<sub>3</sub> (magnetism)

- $\delta$  changes orbital overlaps, hierarchy of magnetic states.
- Extract TB parameters via MLWO, obtain new  $J, K, \Gamma$ .

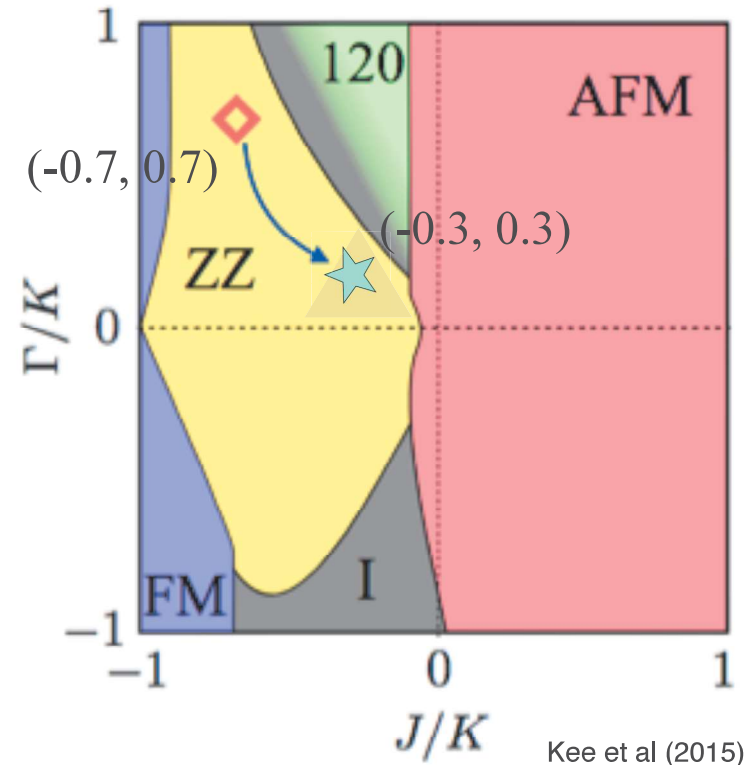


# MINT: graphene on $\alpha$ -RuCl<sub>3</sub> (magnetism)

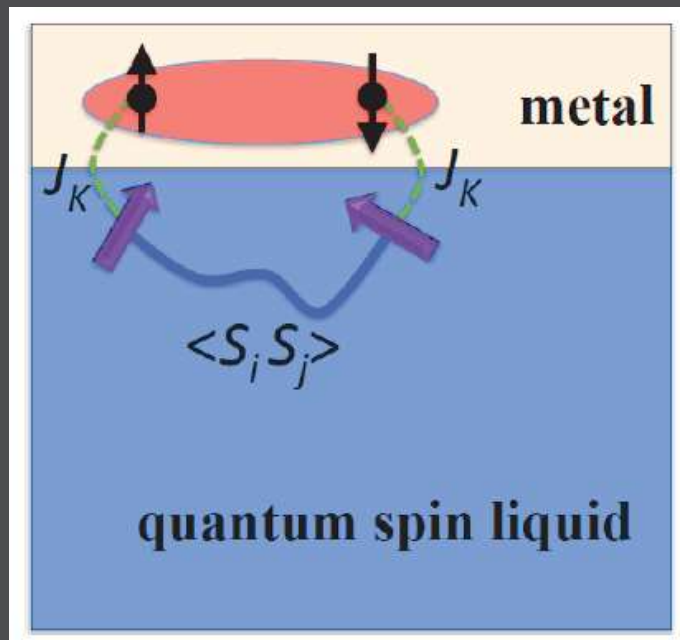
- $\delta$  changes orbital overlaps, hierarchy of magnetic states.
- Extract TB parameters via MLWO, obtain new  $J$ ,  $K$ ,  $\Gamma$ .

System has moved much closer to the origin!

**Stay tuned on experiments:**



# TSC in Metal/Quantum Paramagnet Heterostructures



- Superconductor riding on QSL
- Selection Rule Dictated Intrinsic Topo SC for QSI.
- MINT for g/RuCl<sub>3</sub>:  
Doping!

Gerber, Arias, EAK,  
arXiv: <https://arxiv.org/abs/1902.09550>

# Strategy III

Frustrated Systems with  
Strong Coupling

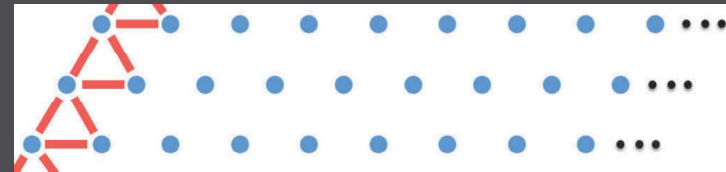
**Density matrix renormalization group study of superconductivity  
in the triangular lattice Hubbard model**

Jordan Venderley and Eun-Ah Kim

*Department of Physics, Cornell University, Ithaca, New York 14850, USA*

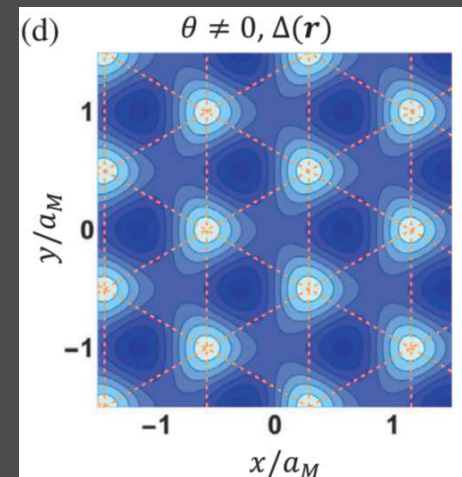
- Model:

$$H = -t \sum_{\langle i,j \rangle \sigma} c_{i\sigma}^\dagger c_{j\sigma} - \mu \sum_{i\sigma} n_{i\sigma} + U \sum_i n_{i\uparrow} n_{i\downarrow}$$



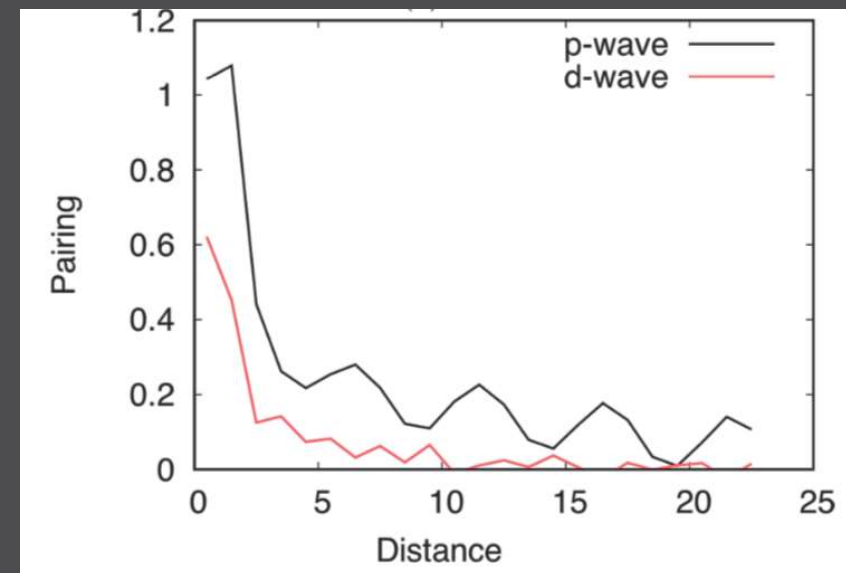
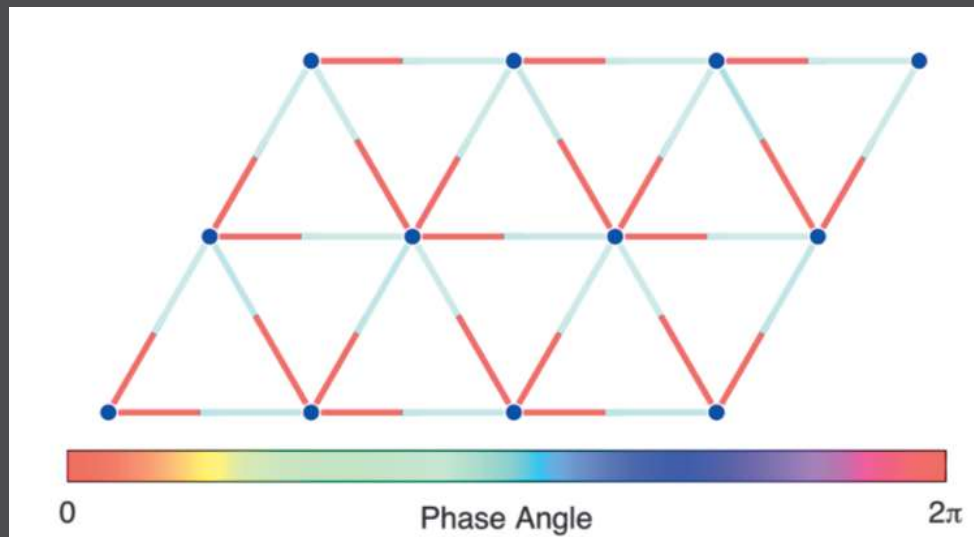
- Materialization?  
Twisted hetero-TMD

Wu, MacDonald et al, PRL 121, 026402 (2018)



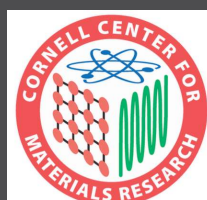
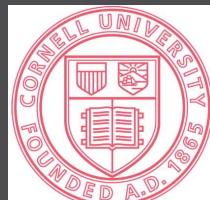
# Pairing Response to Random Edge Pair Field

$$\Delta_{ij}^{\text{singlet}} = \langle c_{i\uparrow}^\dagger c_{j\downarrow}^\dagger - c_{i\downarrow}^\dagger c_{j\uparrow}^\dagger \rangle,$$
$$\Delta_{ij}^{\text{triplet}} = \langle c_{i\uparrow}^\dagger c_{j\downarrow}^\dagger + c_{i\downarrow}^\dagger c_{j\uparrow}^\dagger \rangle.$$



# Designing 2D topological SC's

- Spin-valley locking: hole-doped TMD,  
Hsu et al, Nat. Comm 8, 14985 (2017)
- Quantum Paramagnet Heterostructure:  
She et al, npj Quantum Materials, 2, 64 (2017)  
Gerber et al, arXiv: 1902.09550
- Correlated Triangular Lattice: e.g., hetero TMD bilayer  
Venderley & Kim, PRB 100, 060506 (R)(2019)



ARADIM